

03 May 1994

<p style="text-align: center;"><b>AGS Complex Machine Studies</b>  <b>(AGS STUDIES REPORT Number 313)</b>  <u>Measurement of <math>d(h \cdot f_{rev})/dR</math> and <math>\xi_h</math></u></p>	
<b>Study Period:</b>	10 April 1994, 9:00 am - 21:00 pm
<b>Participants:</b>	R. Thern, M. Tanaka, E. Bleser + MCR
<b>MCR:</b>	N. Williams / K. Zeno, P. Carolan / C. Whalen
<b>Reported by :</b>	M. Tanaka
<b>Machine:</b>	AGS_ Accel. on h=8
<b>Beam:</b>	User3, low intensity $3 \times 10^{12}$ ppp, No chromaticity corrections
<b>Tools:</b>	IPM, Orbit PUE's, Tune Meter, HP5371A Frequency Analyzer Gauss Clock.
<b>Aim:</b>	<i>To Measure <math>Q_h</math> and <math>h \cdot f_{rev}</math> vs <math>\langle x \rangle_{pue}</math>, <math>x(c5)_{ipm}</math> at various times</i>

## I. Introduction

During the machine studies[MS] period in March and early April, we observed substantial large closed orbit distortions throughout the AGS cycle, which varied from -28 mm to +16 mm, peaking around E20[L. Ahrens]. Therefore, previous to this study a few selected main magnets were moved as the first step to reduce the orbit distortions [E. Bleser]. The main purposes of this study are as follows:

- to get AGS orbit data for the next magnet move,
- to measure the mean radius  $\langle x \rangle_{pue} = \langle R \rangle$  from PUE's and  $x(c5)$  from IPM for calibration,
- to measure  $d[h \cdot f_{rev}]/d\langle x \rangle$  and the chromaticity  $\xi_h = \Delta Q_h/(\Delta p/p)$ ,

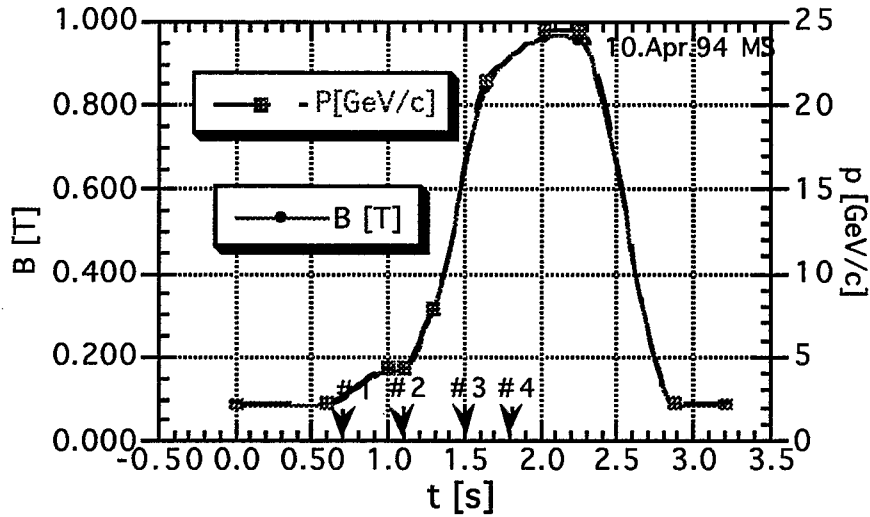
at various times and radius, and to compare the results with MAD predictions to understand the basic machine performance.

## II. Setup and Data Taking

The stored commands for the FY94/SEB setup were reloaded and executed after recovering the polarized proton MS. The data were taken at 4 different times as shown in figure 1:

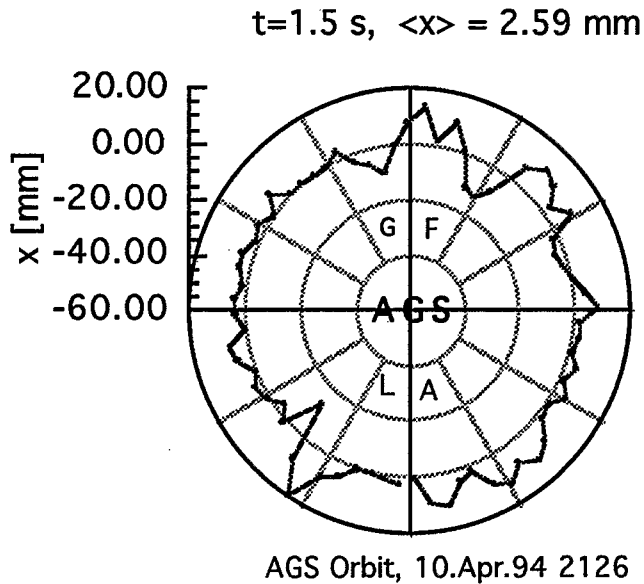
Data#1 at  $t = 0.7$  s from  $t_0$ ,  $p = 2.632$  GeV/c (from Gauss clock counts by IPM)<sup>†</sup>,  
 Data#2 at  $t = 1.1$  s,  $p = 4.278$  GeV/c,  
 Data#3 at  $t = 1.5$  s,  $p = 16.942$  GeV/c,  
 Data#4 at  $t = 1.7$  s,  $p = 21.926$  GeV/c.

<sup>†</sup>  $p = 2.33 + 0.00050568 \cdot GC$  [GeV/c]



**Fig.1. AGS main magnet setup.**

During the data taking, high field chromaticity sextupoles were turned off to minimize possible non-linear effects. The circulating beam intensity was  $2\text{-}3 \cdot 10^{12}$  ppp. This note analyzes the two after\_transition data sets #3 and #4 since these sets are more complete and reliable than #1 and #2. *e.g.*, we started loosing some of the beam when  $\langle x \rangle_{\text{pue}} < -10$  mm or  $\sim +5$  mm at  $t = 0.7$  s and had a difficulty with tune measurements.



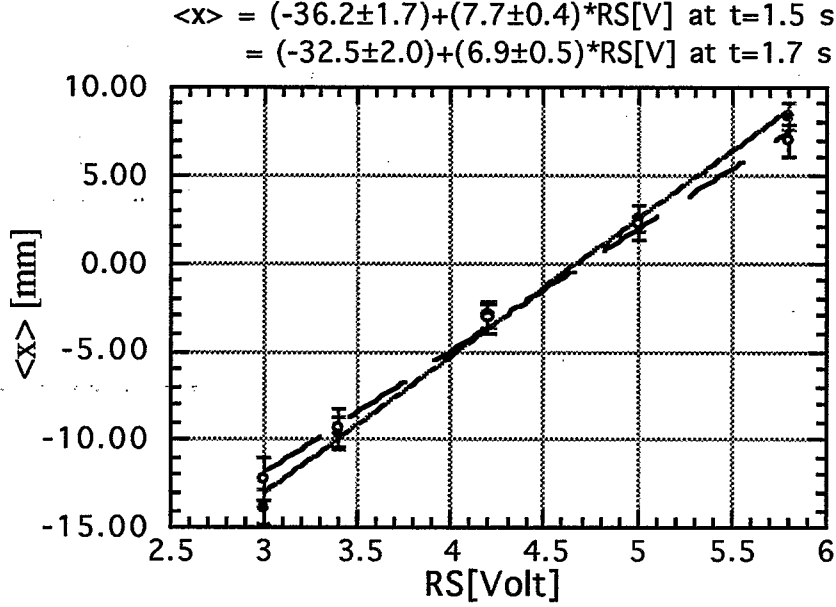
**Fig.2. A typical AGS Orbit at  $t = 1.5$  s during this MS.**

Figure 2 shows a typical AGS orbit during the MS. All the  $\langle x \rangle_{\text{pue}}$  values and its errors were recalculated by removing apparent bad PUE's from a single pulse measurement.

➤ PUE's are located at straight sections 2,4,8,12,14,18 where  $\beta_x$  and  $D_x$  are at average while IPM is located at straight section C5 where  $\beta_x$  and  $D_x$  are at maximum. There were ~62 good ones out of 70 PUE's.

➤ It should be noted that the peak-to-peak variation was reduced by about 50 % to  $\pm \sim 13\text{mm}$  from the unwanted orbit distortions before the MS. This value is still substantially high since the ideal orbit should be less than  $\pm 3\text{-}5\text{ mm}$ . Two extreme points in superperiod K are likely due to unstable PUE's.

The mean beam radius  $\langle x \rangle$  was varied from about  $-13\text{ mm}$  to  $+7\text{ mm}$  by changing the voltage of the radial shifter [RS] as shown in figure 3.



**Fig.3.  $\langle x \rangle_{\text{pue}}$  vs RS[V] at  $t = 1.5$  and  $1.7\text{ s}$ .**

### III. Results and Analysis

All results are summarized in figures 3, 4 and 5 with MAD predictions using the momentum from the gauss clock counts and actual high field quads currents  $\{IQ_h, IQ_v\} = \{100\text{A}, 150\text{A}\}$ . The  $\langle x \rangle_{\text{mad}}$  is calculated by

$$\langle x \rangle_{\text{mad}} = \Delta R = \alpha_p \cdot R \cdot (\Delta p/p),$$

where  $\alpha_p$  is the compaction factor and  $R = 128.452\text{ m}$ . is the reference mean radius of the AGS. The  $h \cdot f_{\text{rev}}$  is calculated by

$$h \cdot f_{\text{rev}} = 8 \cdot c \cdot (p/E) / (2\pi \cdot (R + \Delta R)),$$

where  $h = 8$ , the rf harmonic number,  $c$  = speed of light and  $p/R = \beta_{\text{rel}}$ .

### III.A $\langle x \rangle_{\text{pue}}$ vs $x(c5)_{\text{ipm}}$

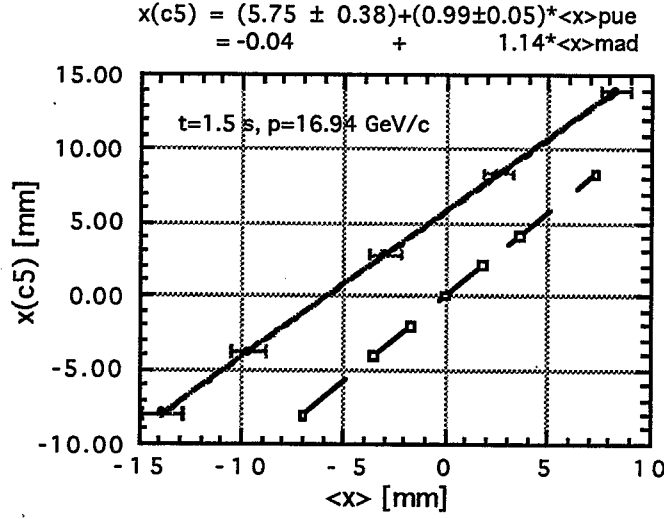


Fig. 3a.

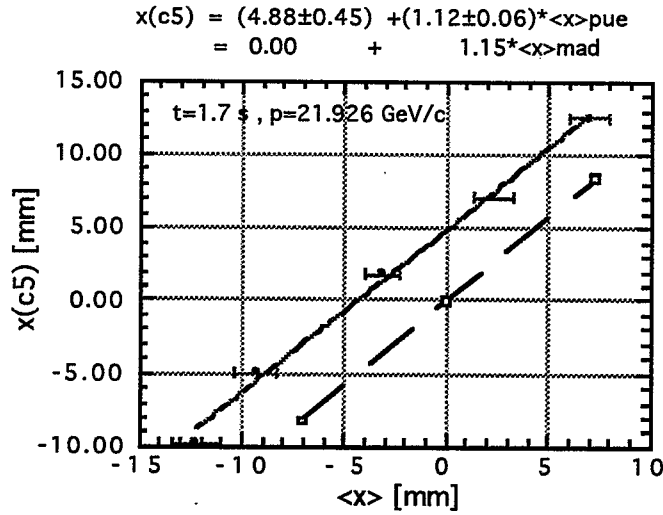


Fig. 3b.

**Fig.3.  $x(C5)$  vs  $\langle x \rangle$  with MAD predictions at  $p = 16.942$  and  $21.926 \text{ GeV/c}$ .**

Figure 3 shows the results from the PUE's and the IPM. It displays a linear relationship between  $x(c5)_{\text{ipm}}$  and  $\langle x \rangle_{\text{pue}}$ . If the  $x(c5)_{\text{ipm}} = 0$  corresponds to the central orbit, the central orbit mean radius is at the  $\langle x \rangle_{\text{pue}} = -5.3 \pm 0.3 \text{ mm}$ . The MAD predicted value of  $dx(c5)_{\text{ipm}}/d\langle x \rangle_{\text{pue}}$  is in excellent agreement with the data at  $p=21.926 \text{ GeV/c}$  but in poor agreement with one at  $p=16.942 \text{ GeV/c}$ .

It is generally assumed that  $\langle x \rangle_{\text{pue}} = -4.0 \text{ mm}$  corresponds to the central orbit mean radius.

### III.B $h^*f_{rev}$ vs $\langle x \rangle_{pue}$

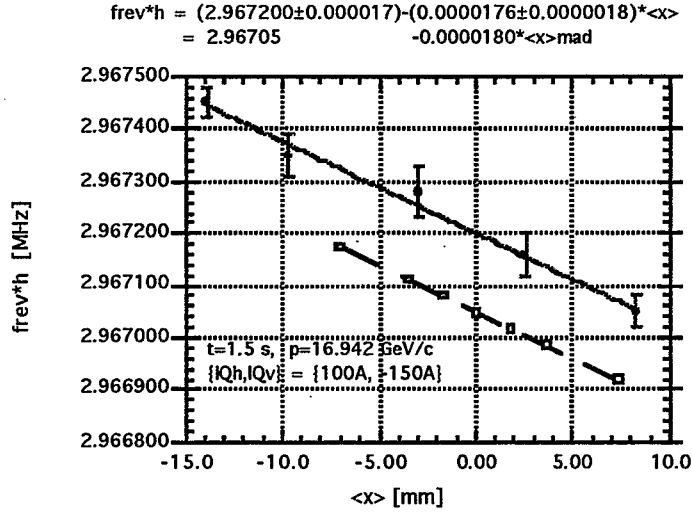


Fig. 4a.

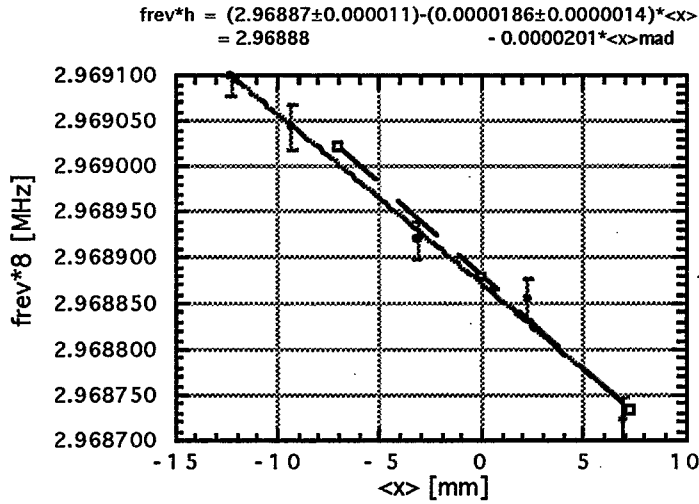


Fig. 4b

**Fig.4.  $h^*f_{rev}$  vs  $\langle x \rangle$  with MAD predictions.**

The MAD predictions of  $d(h^*f_{rev})/d\langle x \rangle$  are in excellent agreement with both data. Some of the absolute differences in  $h^*f_{rev}$  (~100-240 Hz), could be attributed to the systematic errors in calculating the momentum from Gauss clock counts by 0.5-1.0 %. The Gauss clock calibration could be wrong by 1.8 % [M. Brennan].

### III.C $Q_h$ vs $dp/p$

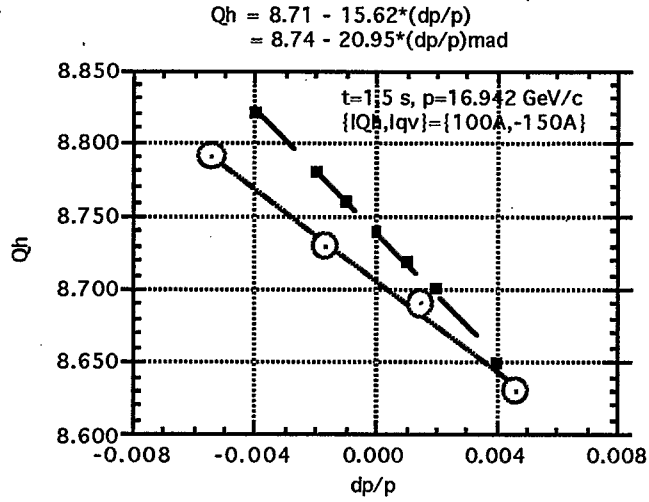


Fig. 5a.

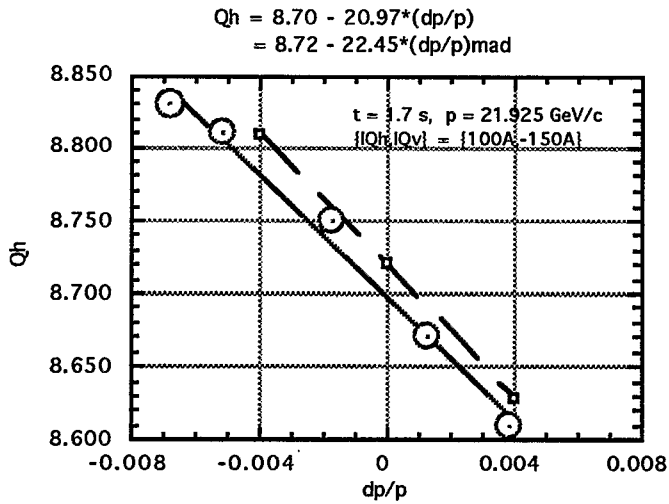


Fig. 5b.

**Fig.5.  $Q_h$  vs  $dp/p$  with MAD predictions.**

Figure 5a and 5b show  $Q_h$  vs  $dp/p$  at  $p=16.942$  and  $21.926 \text{ GeV/c}$ , respectively, where  $dp/p = \langle x \rangle / (\alpha_p R)$ . The measured  $Q_v$  value stays constant to be  $8.83 \pm 0.01$  while the MAD predicts  $Q_v = 8.82 \pm 0.03$ . Big circles for measured  $Q_h$  indicate that we had some difficulties in measuring  $Q_h$ . In the FFT display, there were several broad peaks between 8.5 and 9.0 and each peak had its substructure. At  $p = 21.926 \text{ GeV/c}$ , the measured chromaticity  $\xi_h = 21.0$  is in good agreement with the MAD prediction of 22.5 but not for the  $p=16.942 \text{ GeV/c}$  data.

## IV. Conclusions

- The two data sets on the horizontal tune[ $Q_h$ ] and the rf frequency [ $h \cdot f_{rev}$ ] vs the mean radius[ $\langle x \rangle < \pm 10$  mm] at  $p = 16.942$  and  $21.926$  GeV/c with low intensity proton beam without chromaticity corrections were analyzed and compared with the MAD predictions.
- Despite the fact that the machine was not well tuned yet and we had some difficulties in measuring tunes, the data indicate that the AGS behaved linearly as expected.
- It would be interesting to perform similar measurements at the following conditions:

- at the well-tuned machine,
- at higher momentum(e.g., 25, 27, 29 GeV/c)
- with higher intensity beam(e.g., 10, 20, 30 TP),
- using well prepared and calibrated tools,
- increasing the radial steering range from  $\pm 10$  to  $\pm 25$  mm (and beyond until beam losses occur),
- with chromaticity sextupoles off and on,
- also measuring the transverse beam emittance and the momentum spread,
- etc,

and knowing the machine conditions well (e.g.,  $\gamma_{tr}$ -jump, VHF, transverse damper, bumps etc.)